

# POPULATION PHARMACOKINETICS

Raymond Miller, D.Sc.  
Daiichi Sankyo Pharma Development

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## Population Pharmacokinetics

Definition

Advantages/Disadvantages

Objectives of Population Analyses

Impact in Drug Development

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## Definition

Population pharmacokinetics describe

- The typical relationships between physiology (both normal and disease altered) and pharmacokinetics/pharmacodynamics,
- The interindividual variability in these relationships, and
- Their residual intraindividual variability.

Sheiner-LB  
Drug-Metab-Rev. 1984; 15(1-2): 153-71

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### Definition

E.g.: A simple PK model

$$C_p = \frac{R_i}{Cl} \cdot \left( 1 - e^{-kt} \right) \pm \varepsilon$$

$R_i$  = infusion rate  
 $Cl$  = drug clearance  
 $k$  = elimination rate constant  
 $\varepsilon$  = measurement error, intra-individual error  
 $\varepsilon \approx N(0, \sigma)$

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### Definition

$$C_p = \frac{R_i}{Cl} \cdot \left( 1 - e^{-kt} \right) \pm \varepsilon$$

$$C_p = C_{p_{ss}} \cdot e^{-kt} \pm \varepsilon$$

$$Cl = \frac{R_i}{C_{p_{ss}}} \pm \varepsilon$$


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### Definition

$Cl$  = metabolic clearance + renal clearance  
 $Cl = \Theta_1 + \Theta_2 \cdot CCr \pm \eta$

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### Definition

Cl = metabolic clearance + renal clearance

$$Cl = \theta_1 + \theta_2 \cdot CCr \pm \eta$$

$\eta \approx N(0, \omega)$

The figure shows a scatter plot with 'Creatinine Clearance' on the x-axis and 'Drug Clearance' on the y-axis. A blue regression line is drawn through several data points. A normal distribution curve is overlaid on the plot, centered around the regression line, representing the error term  $\eta$ . A circle highlights the error term in the equation above.

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Graphical illustration of the statistical model used in NONMEM for the special case of a one compartment model with first order absorption. (Vozech et al. Eur J Clin Pharmacol 1982;23:445-451)

The graph plots  $\log C$  on the y-axis against Time on the x-axis. It shows a population mean curve and several individual subject curves. Labels include:
 

- subject 1:  $\bar{Cl} = \theta_1 + \eta_{21k}$ ,  $\bar{V} = \theta_3 + \eta_{3k}$
- subject 2:  $\bar{Cl} = \theta_1 + \eta_{22k}$ ,  $\bar{V} = \theta_3 + \eta_{3k}$
- Population mean:  $\bar{Cl}$ ,  $\bar{Cl}$ ,  $\bar{V}$
- Interindividual variability
- Intraindividual variability (I.I.)
- total residual error

 The equation  $\bar{Cl} = \theta_1 + \eta_{21k} + \theta_2 + \eta_{22k} + Cl_{cr}$  is also shown.

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### Objectives

1. Provide Estimates of Population PK Parameters (CL, V) - Fixed Effects
2. Provide Estimates of Variability - Random Effects
  - Intersubject Variability
  - Interoccasion Variability (Day to Day Variability)
  - Residual Variability (Intrasubject Variability, Measurement Error, Model Misspecification)

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### Objectives

#### 3. Identify Factors that are Important Determinants of Intersubject Variability

- *Demographic*: Age, Body Weight or Surface Area, gender, race
- *Genetic*: CYP2D6, CYP2C19
- *Environmental*: Smoking, Diet
- *Physiological/Pathophysiological*: Renal (Creatinine Clearance) or Hepatic impairment, Disease State
- *Concomitant Drugs*
- *Other Factors*: Meals, Circadian Variation, Formulations

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### Advantages

- Sparse Sampling Strategy (2-3 concentrations/subject)
  - Routine Sampling in Phase II/III Studies
  - Special Populations (Pediatrics, Elderly)
- Large Number of Patients
  - Fewer restrictions on inclusion/exclusion criteria
- Unbalanced Design
  - Different number of samples/subject
- Target Patient Population
  - Representative of the Population to be Treated

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### Disadvantages

- Quality Control of Data
  - Dose and Sample Times/Sample Handling/ Inexperienced Clinical Staff
- Timing of Analytical Results/Data Analyses
- Complex Methodology
  - Optimal Study Design (Simulations)
  - Data Analysis
- Resource Allocation
- Unclear Cost/Benefit Ratio

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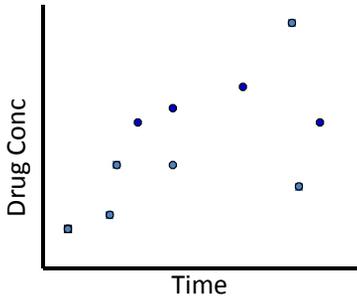
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Models are critical in sparse sampling situations:



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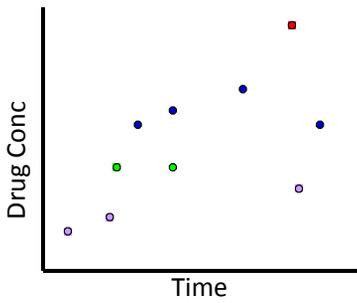
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Models are critical in sparse sampling situations:



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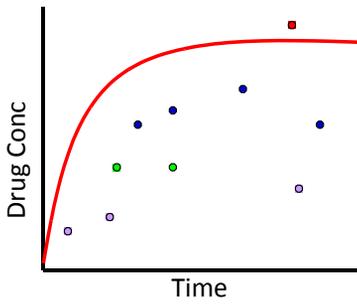
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Models are critical in sparse sampling situations:



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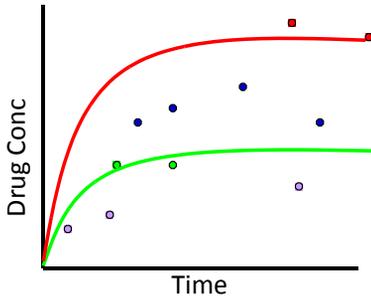
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Models are critical in sparse sampling situations:



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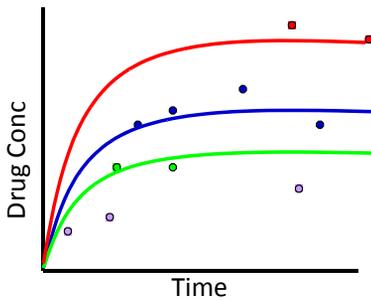
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Models are critical in sparse sampling situations:



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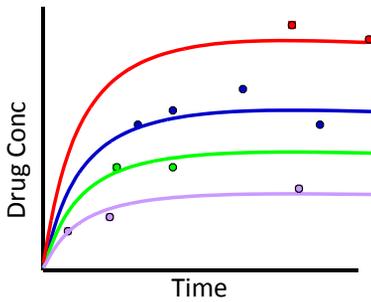
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Models are critical in sparse sampling situations:



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### Study Objectives

- To evaluate the efficacy of drug treatment or placebo as add on treatment in patients with partial seizures.

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### Data Structure

Study	N	Doses Explored
1	308	0, 600 mg/day (bid & tid)
2	287	0, 150, 600 mg/day (tid)
3	447	0,50,150,300,600 mg/day (bid)
Total	1092	

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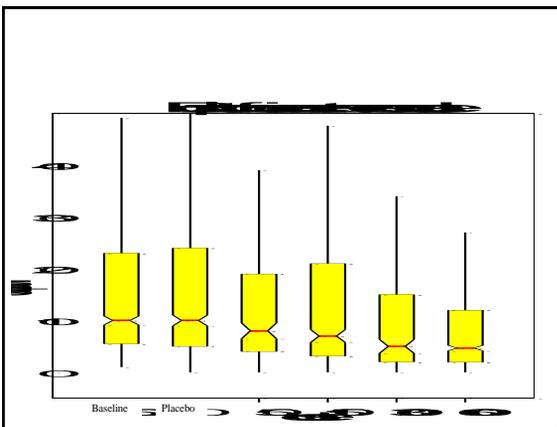
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Count Model

$$P(Y_i = x) = e^{-\lambda} \frac{\lambda^x}{x!}$$

$\lambda$  represents the expected number of events per unit time

$$E(Y_{ij}) = \lambda_i t_{ij}$$

The natural estimator of  $\lambda$  is the overall observed rate for the group.

$$\lambda = \frac{\text{Total counts}}{\text{Total time}}$$

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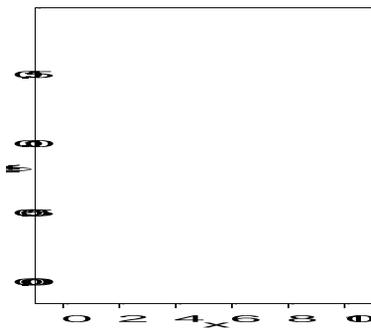
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Suppose there are typically 5 occurrences per month in a group of patients:  $\lambda=5$   $P(Y_i = x) = e^{-\lambda} \frac{\lambda^x}{x!}$



X=	Pr(Y=x)
0	0.007
1	0.034
2	0.084
3	0.140
4	0.175
5	0.180
6	0.150
7	0.104
8	0.065
9	0.036
10	0.018

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$$P(Y_i = x) = e^{-\lambda} \frac{\lambda^x}{x!}$$

The mean number of seizure episodes per month ( $\lambda$ ) was modeled using NONMEM as a function of drug dose, placebo, baseline and subject specific random effects.

$$\lambda = \text{Baseline} + \text{placebo} + \text{drug} + \eta$$

Baseline = estimated number of seizures reported during baseline period

Placebo = function describing placebo response

Drug = function describing the drug effect

$\eta$  = random effect

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### Initial Model

$$\lambda = \text{BASE} \cdot \left( 1 - \frac{E_{\max} \cdot D}{ED_{50} + D} - \text{PLAC} \right) \cdot e^{\eta_1}$$

$$\lambda = 10.8 \cdot \left( 1 - \frac{0.38 \cdot D}{48.7 + D} - 0.1 \right) \cdot e^{\eta_1}$$

BASE=10.8 (9.9,11.7)
ED <sub>50</sub> = 48.7 (0,129.1)
E <sub>max</sub> = 0.38 (0.15,0.61)
PLAC=0.1(-0.22,0.02)
σ <sub>η</sub> = 1.1 (1.0,1.18)

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### Sub-population analysis

- Some patients are refractory to any particular drug at any dose.
- Interest is in dose-response in patients that respond
- Useful in adjusting dose in patients who would benefit from treatment
- Investigate the possibility of at least two sub-populations.

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### Mixture Model

A model that implicitly assumes that some fraction  $p$  of the population has one set of typical values of response, and that the remaining fraction  $1-p$  has another set of typical values

#### Population A ( $p$ )

$$\lambda_1 = \text{Baseline}_1 + \text{placebo}_1 + \text{drug}_1 + \eta_1$$

#### Population B ( $1-p$ )

$$\lambda_2 = \text{Baseline}_2 + \text{placebo}_2 + \text{drug}_2 + \eta_2$$

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Final Model

Population A = 75%

$$\lambda = 11.1 \cdot \left( 1 - \frac{1 \cdot Dose}{186 + Dose} \cdot D_1 - 0.11 \cdot D_0 \right) \cdot e^{\eta_1}$$

Population B = 25%

$$\lambda = 15.1 \cdot (1 + 0.26 \cdot D_1 + 1.44 \cdot D_0) \cdot e^{\eta_2}$$

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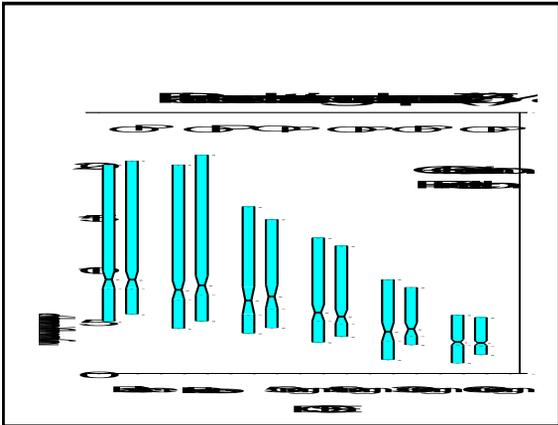
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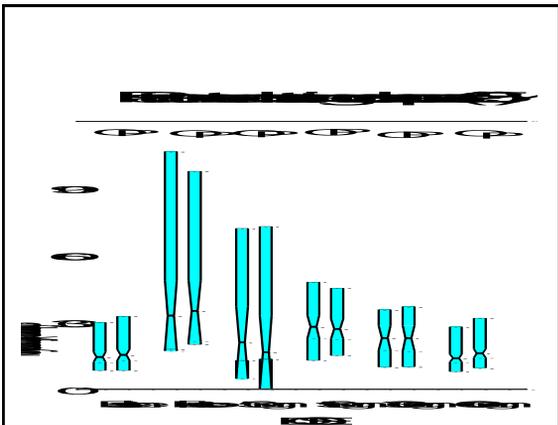
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### Expected percent reduction in seizure frequency

- Monte Carlo simulation using parameters and variance for Subgroup A
- 8852 individuals (51% female)
- % reduction from baseline seizure frequency calculated
- Percentiles calculated for % reduction in seizure frequency at each dose

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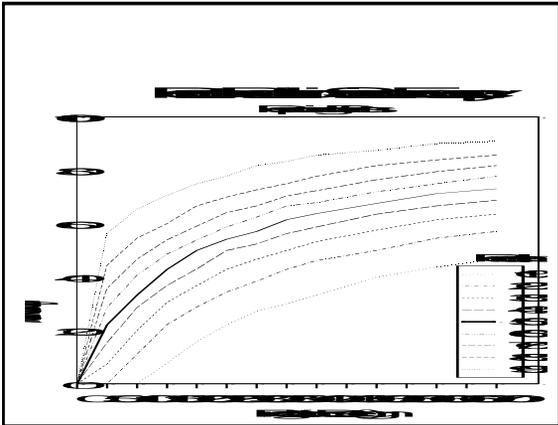
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### Results

Parameter	Parameter Estimates (95% CI)	
	Gabapentin	Pregabalin
Base <sub>A</sub> (seizures/month)	14.0 (12.4,15.6)	11.1 (10.2,12.0)
Base <sub>B</sub> (seizures/month)	16.8 (8.8,24.8)	15.1 (12.3,17.9)
E <sub>max A</sub> (maximal fractional change)	-0.25 (-0.31, -0.18)	-1.0
E <sub>max B</sub> (maximal fractional change)	2.34 (0.20,4.48)	0.26(-0.15,0.66)
Placebo <sub>A</sub> (maximal fractional change)	-0.15 (-0.29, -0.009)	-0.11 (-0.18, -0.03)
Placebo <sub>B</sub> (maximal fractional change)	4.34 (-0.80,9.47)	1.44 (0.66,2.22)
ED <sub>50</sub> (mg)	463.0 (161.3,764.7)	186.0 (91.4,280.6)
Proportion <sub>A</sub>	0.95 (0.93,0.98)	0.75(0.61,0.88)

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## Conclusions

- A comparison of the dose-response relationship for gabapentin and pregabalin reveals that pregabalin was 2.5 times more potent, as measured by the dose that reduced seizure frequency by 50% (ED50).
- Pregabalin was more effective than gabapentin based on the magnitude of the reduction in seizure frequency (Emax)
- Three hundred clinical trials for each drug were simulated conditioned on the original study designs. Each simulated trial was analyzed to estimate % median change in seizure frequency. The observed and model-predicted treatment effects of median reduction in seizure frequency for gabapentin and pregabalin are illustrated for all subjects and for responders. Data points represent median percentage change from baseline in seizure frequency for each treatment group (including placebo). The shaded area corresponds to predicted 10th and 90th percentiles for median change from baseline in seizure frequency.

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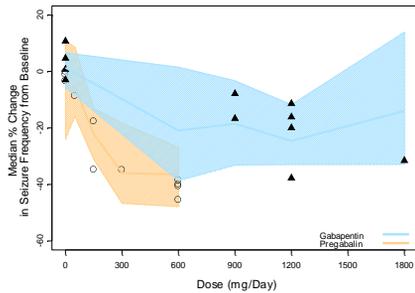
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Relationship Between %Change in Seizure Frequency (Relative to Baseline) and Daily Dosage of Gabapentin and Pregabalin




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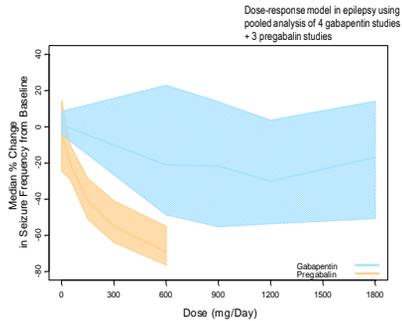
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Relationship Between %Change in Seizure Frequency (Relative to Baseline) and Daily Dosage of Gabapentin and Pregabalin in Responders to Treatment




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### Clinical Trial Simulation

- Used to assess how different design and drug factors may affect trial performance.
- May be viewed as an extension of statistical design evaluation.

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### Planning Phase 2 POC for Alzheimer's Disease Drug

Because the mechanism of action of CI-1017 was untested clinically, the principle objective of the clinical study was to ascertain whether CI-1017 improved cognitive performance at least as fast and as well as tacrine.

This would be considered proof of concept (POC).

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### Typical Effectiveness Trials (AD)

- Parallel group design
- Two to four treatment groups + placebo
- Powered to detect 3 point improvement in ADAS-Cog
- Minimum 12 weeks of treatment

– Require about 80 subjects per dose group to have 90% power (2 sided 50% sig. Level)

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## DATA EVALUATION

- DOES THE DRUG WORK?
  - AOV to test null hypothesis of no drug effect
  - Rejection of null hypothesis judged correct
  - Dose trend test
- IS THE SHAPE MONOTONIC OR U-SHAPED?
  - Similar to the above two steps
  - Non-positive trial pattern classified as flat
  - Inference between monotonic and u-shaped based on highest dose having best mean outcome.

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## SIMULATION

- 100 Trial simulations
- Pharsight trial simulator (TS2)
- Data from each trial analyzed
- Conclusions scored

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## DRUG EFFECT

**Percent of 100 trials (power) that detected a drug effect for design number 6, 7 and 8.**

Design number	6	7	8
Dose response shape			
Linear	84	41	51
Flat	88	58	67
Step	96	75	85
U-shape	57	40	49
AVERAGE	82	54	63

Design number 6: 4x4 Latin Square, 3 weeks per treatment.  
 Design number 7: 4x4 Latin Square with 2 parallel groups.  
 Design number 8: 4x4 Latin Square, 4 weeks per treatment.

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## SHAPE

**Percent of 100 trials (power) that correctly identified dose-response shape for design number 6, 7 and 8**

Design number	8	7	6
Dose response shape			
Linear	96	69	72
Emax	84	62	74
Smax	96	83	89
U-shape	45	34	39
AVERAGE	80	62	69

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### Simulation Conclusions

#### Design

- 4x4 LS with 4-week periods using bi-weekly measurements
  - Was best among alternatives considered for detecting activity and identifying DR shape
  - Met minimum design criteria (80% average power)

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### Results

- 4x4 LS design was accepted, conducted, and analyzed more-or-less as recommended
- Unfortunately, drug didn't work
  - But we were able to find this out more quickly and with less resources than with conventional design

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**Gabapentin – Neuropathic Pain  
NDA**

- Two adequate and well controlled clinical trials submitted.
- Indication – post-herpetic neuralgia
- Trials used different dose levels
  - 1800 mg/day and 2400 mg/day
  - 3600 mg/day
- The clinical trial data was not replicated for each of the dose levels sought in the drug application

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**FDAMA 1997**

FDA review staff decided to explore whether PK/PD analyses could provide the confirmatory evidence of efficacy.

“—based on relevant science, that data from one adequate and well controlled clinical investigation and confirmatory evidence (obtained prior to or after such investigation) are sufficient to establish effectiveness.”

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**Gabapentin Study Designs for PHN**

Overview of PHN Controlled Studies: Double-Blind Randomized/Target Dose and ITT Population

Duration of Double-Blind Phase			Number of Patients							
Titration	Fixed Dose	Overall Duration	Placebo	Final Gabapentin Dose, mg/day				Any Gabapentin	All Patients	
				600	1200	1800	2400			3600
4 Weeks	4 Weeks	8 Weeks	116	--	--	--	--	113	113	229
3 Weeks	4 Weeks	7 Weeks	111	--	--	115	108	--	223	334
4 Weeks	4 Weeks	8 Weeks	152	--	--	--	153	--	153	305
			379	0	0	115	261	113	489	868

<sup>†</sup> included in study design  
 All randomized patients who received at least one dose of study medication.

- Used all daily pain scores (27,678 observations)
- Exposure-response analysis included titration data for within-subject dose response

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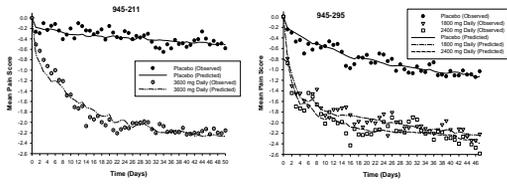
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### Gabapentin Response in PHN



Time Dependent Placebo Response, Emax Drug Response and Saturable Absorption,

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### Results

- Summary statistics showed pain relief for both studies at different doses concur.
- M & S showed pain scores for both studies can be predicted with confidence from the comparative pivotal study (cross confirming).

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### Conclusion

- The use of PK/PD modeling and simulation confirmed efficacy across the three studied doses, obviating the need for additional clinical trials.
- Gabapentin was subsequently approved by FDA for post-herpetic neuralgia
- The package insert states “pharmacokinetic/pharmacodynamic modeling provided confirmatory evidence of efficacy across all doses”

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### Issue

- A new  $\alpha_2\delta$  ligand (PD0332334) that has anxiolytic properties was in development.
- Little was known about AE's for this compound, however, extensive knowledge from other  $\alpha_2\delta$  ligands (pregabalin) available.
- It is generally believed that dose titration may reduce AE's.

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### Questions

- Would AE frequency be different if the drug was titrated to the target dose?
- How long do we need to titrate to minimize AE's?
- How many dose steps do we need to minimize AE's?

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### Objectives

- To describe the exposure-longitudinal AE severity relationship following multiple doses of pregabalin.
- To describe the relationship between AE and patient dropout
- To explore the relationship between dose titration of pregabalin and dropout

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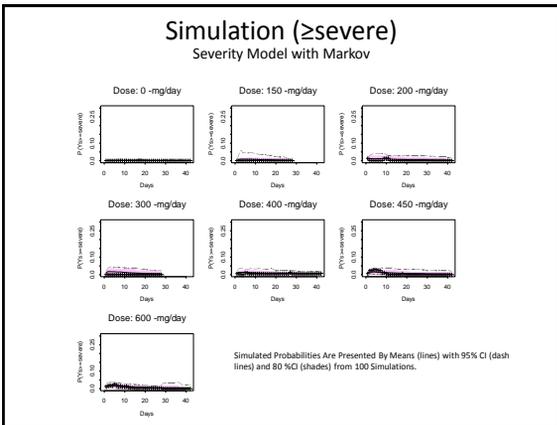
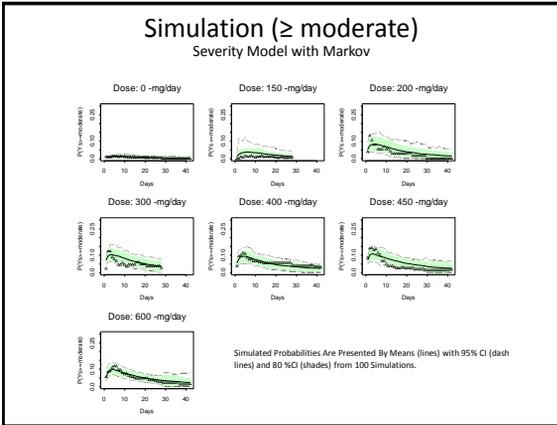
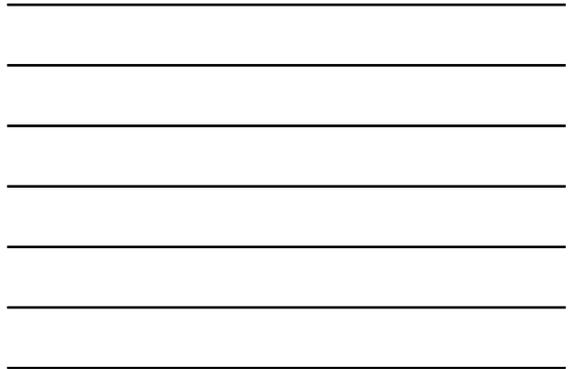
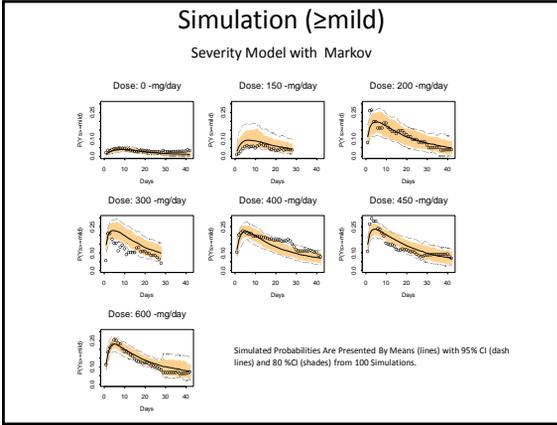
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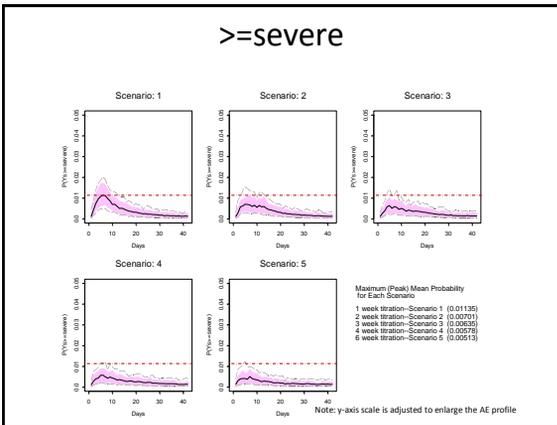
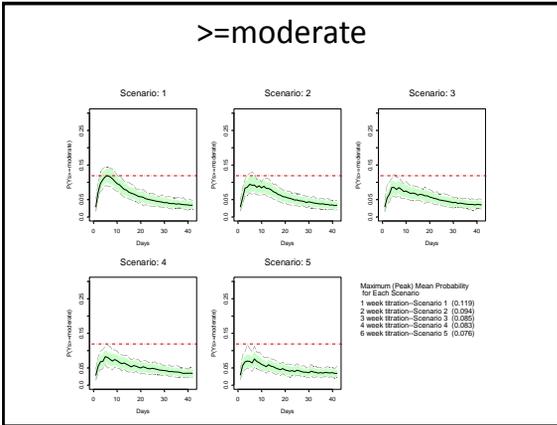
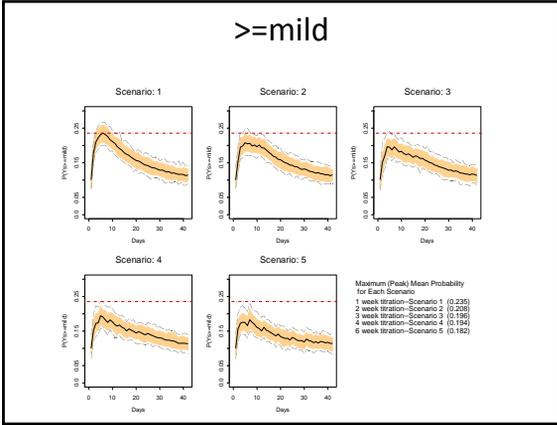
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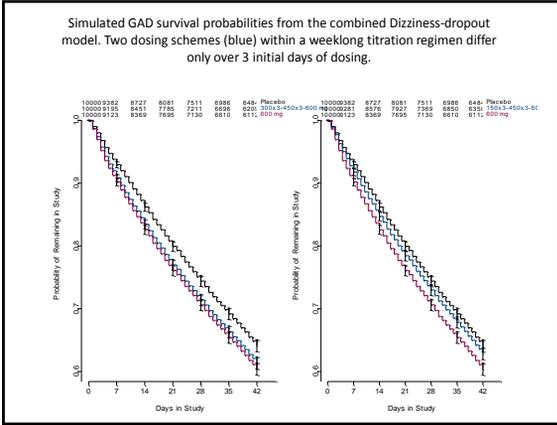
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### Summary

- Population PK/PD quantifies and allows prediction of the variability in drug response in the population of interest.
- It enables optimizing the dosage regimen in the target population.
- Population PK/PD is an essential tool to improve the efficiency and to facilitate decision making in drug development and regulatory assessment.

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